Syllabus: Axiomatic construction of the theory of probability, independence, conditional probability, and basic formulae, random variables, probability distributions, functions of random variables; Standard univariate discrete and continuous distributions and their properties, mathematical expectations, moments, moment generating function, characteristic functions; Random vectors, multivariate distributions, marginal and conditional distributions, conditional expectations; Modes of convergence of sequences of random variables, laws of large numbers, central limit theorems.

Definition and classification of random processes, discrete-time Markov chains, Poisson process, continuous-time Markov chains, renewal and semi-Markov processes, stationary processes, Gaussian process, Brownian motion, filtrations and martingales, stopping times and optimal stopping.

Texts:

- 1. P. G. Hoel, S. C. Port and C. J. Stone, Introduction to Probability Theory, Universal Book Stall, 2000.
- 2. J. Medhi, Stochastic Processes, 3rd Ed., New Age International, 2009.
- 3. S. Ross, A First Course in Probability, 6th Ed., Pearson Education India, 2002.

References:

- 1. G.R. Grimmett and D. R. Stirzaker, Probability and Random Processes, Oxford University Press, 2001.
- 2. W. Feller, An Introduction to Probability Theory and its Applications, Vol. 1, 3rd Ed., Wiley, 1968.
- 3. K.S. Trivedi, Probability and Statistics with Reliability, Queuing, and Computer Science Applications, Wiley India, 2008.
- 4. S.M. Ross, Stochastic Processes, 2nd Ed., Wiley, 1996.
- 5. C.M. Grinstead and J. L. Snell, Introduction to Probability, 2nd Ed., Universities Press India, 2009.